Project SCooP-Sakura Presentation, Progress, Perspectives NII, Japan, and LINA, France

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### Outline of the presentation

- Context and general presentation of the project
- What is this about?, and what are our objectives?
- Besides constraints, other issues we will have to tackle
- Conclusion and future plans

# Getting acquainted with:

# **SCooP-Sakura**

**SCooP** 

- . Soft and Continuous Constraint Programming
- Cooperative project between NII (Tokyo) and LINA (Nantes)
- Part of the MOU between these institutes
- Objectives of SCooP: integrate all projects related to soft and / or continuous constraints between NII and LINA

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#### **Projects integrated to SCooP**

Speculative Constraint Processing in Multi-Agent Systems
 Members: Ken Satoh, Hiroshi Hosobe, Makoto Yokoo, Katsutoshi
 Hirayama, Martine Ceberio

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- Speculative Constraint Processing in Multi-Agent Systems
- Dynamic CSP

Members: Ken Satoh, Hiroshi Hosobe, Narendra Jussien

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#### **Projects integrated to SCooP**

- Speculative Constraint Processing in Multi-Agent Systems
- Dynamic CSP
- project Sakura

### More about Sakura

# **Continuous Soft Constraints and Graphical Applications**

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Began since first semester of 2004.

# The nuts and bolts of:

# **Project Sakura**

- Motivation
- Objectives
- Framework

**Constraint satisfaction** 

Solving a (set of) constraint(s):

determining the instanciations of the variables (within the specified domains) that meet/satisfy the constraint(s)

#### **Constraint satisfaction**

#### Solving a (set of) constraint(s):

determining the instanciations of the variables (within the specified domains) that meet/*satisfy* the constraint(s)

- = Splitting the search space (*i.e.*, the variables' domains) into:
  - the elements satisfying the constraints (consistent elements)
  - the elements violating the constraints (inconsistent elements)

#### Why be flexible?

1. because constraints may not be compatible: *i.e.*, no instanciation meets the constraints *e.g.*, the model ≠ expected picture of the situation or too ambitious to be consistent etc.

#### Why be flexible?

- 1. because constraints may not be compatible: *i.e.*, no instanciation meets the constraints *e.g.*, the model ≠ expected picture of the situation or too ambitious to be consistent etc.
- 2. because it may make no sense to divide accurately the search space into two precisely bounded parts

e.g., when data not accurate enough, due to machine error ~> meaningless to define an accurate frontier between elements



### **Organizing a meeting with n participants**

## **Organizing a meeting with n participants**

- all participants have a tight schedule
- we know the schedule of each of them: meeting times, time to go from one meeting to the other (known with uncertainty → interval), etc.
- ? is there a time slot, on day d, s.t. all can meet?

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On the other hand:

- this meeting may be held without everybody attending?
- there may be possible other changes in the schedules of participants?
- etc.

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#### Most probably not...

On the other hand:

- this meeting may be held without everybody attending?
- there may be possible other changes in the schedules of participants?
- etc. Many possible adjustments...

Implement a library for handling such inconsistent problems
 objectives of such a tool
 NOT to provide the user with expert advise

Implement a library for handling such inconsistent problems

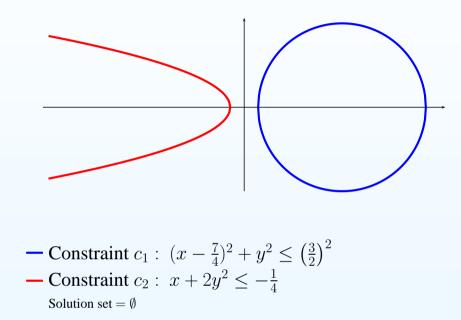
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 BUT to determine solutions<sup>a</sup> corresponding to his/her
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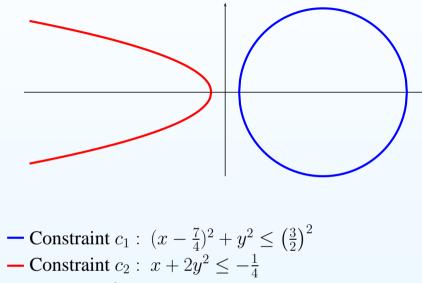
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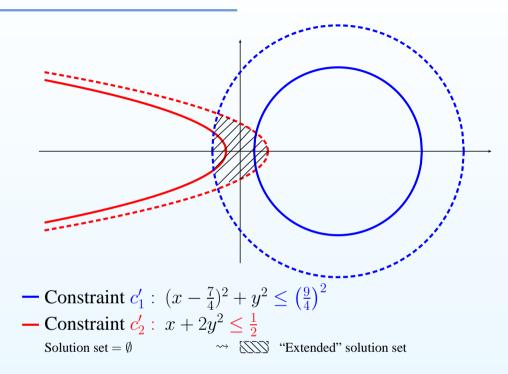
### But then: what kind of flexibility?



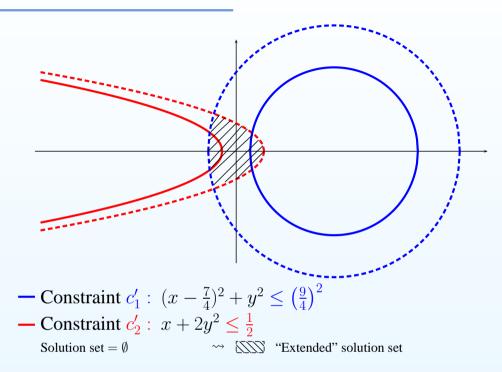


Solution set =  $\emptyset$ 

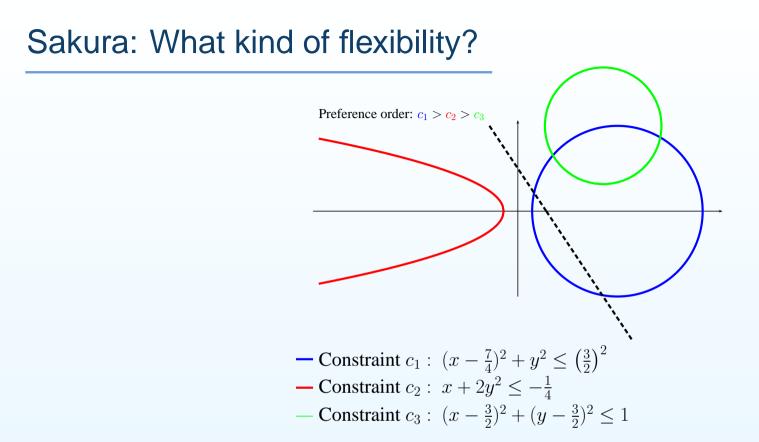
• stretch the constraints



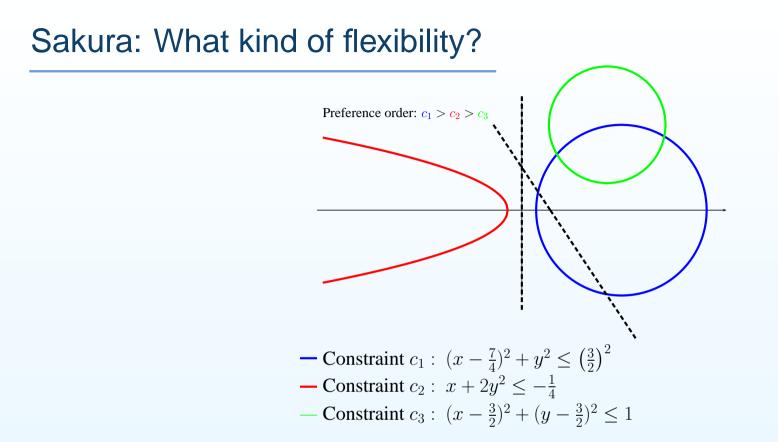
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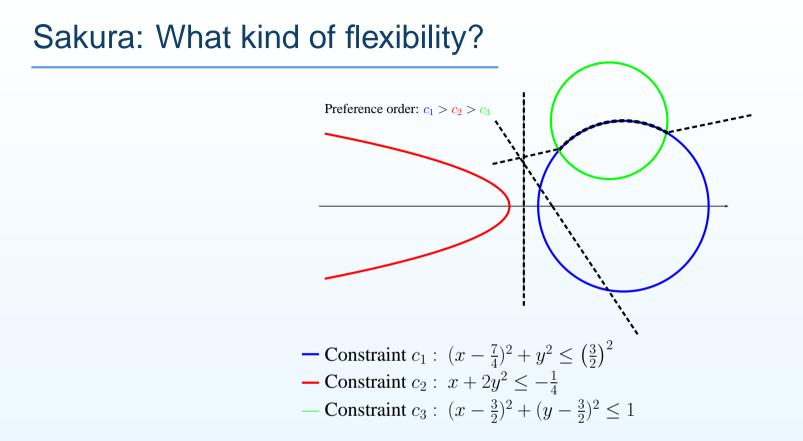
- stretch the constraints
- establish orders, with possible interpretations such as:
  - preferences over the constraints with possible distances



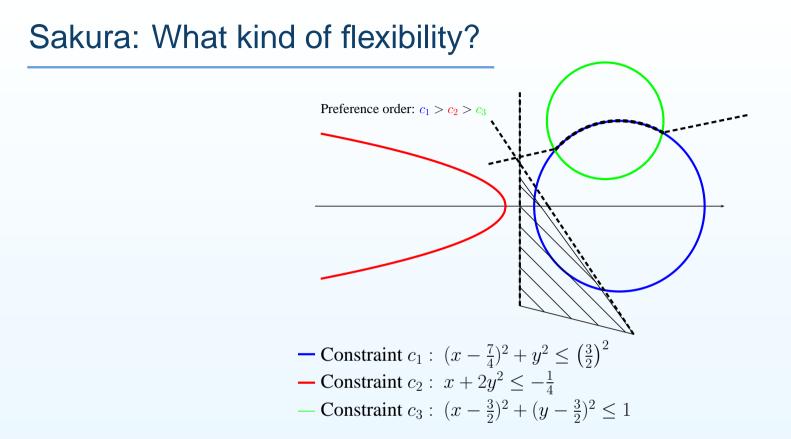
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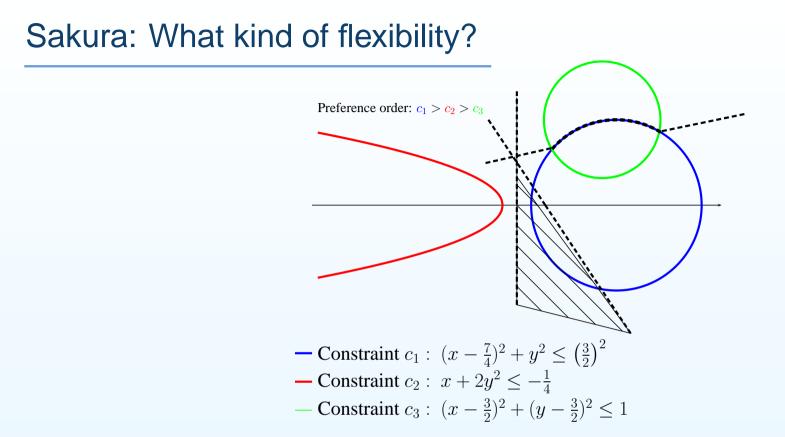
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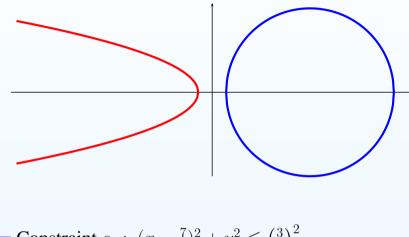
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- stretch the constraints
- establish orders, with possible interpretations such as:
  - preferences over the constraints with possible distances
  - over the constraints as crisp constraints



- Constraint 
$$c_1$$
:  $(x - \frac{7}{4})^2 + y^2 \le \left(\frac{3}{2}\right)^2$   
- Constraint  $c_2$ :  $x + 2y^2 \le -\frac{1}{4}$   
Solution set =  $\emptyset$ 

- stretch the constraints
- establish orders, with possible interpretations such as:
  - preferences over the constraints with possible distances
  - over the constraints as crisp constraints
  - with "if then else" meaning

### Sakura: What kind of flexibility? (cont'd)

- stretch the constraints
- **strong preferences:** order over the satisfaction of the constraints
- weak preferences: order met only if possible
- priorities
- "if then else" Orders: if  $c_1$  then  $c_1 \wedge c_2$ , else  $c_3$
- hierarchies
- etc.

# Sakura: What kind of flexibility? (cont'd)

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Objective:	be general enough
Practically:	we focus on graphical applications
	(cf. Hosobe-sensei's presentation)
Later:	we will enrich our application fields

# Sakura: aim of our work

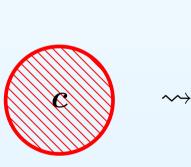
- Based on constraint solving and optimization methods:
  - optimization: minimization of the violation
  - constraint solving: to maintain a preference order + for when non-zero distances to constraints are not allowed
- Be general enough to be able to model many kinds of soft constraints
  - yet we will restrict ourselves to some of them
- Use <u>state-of-the-art</u> solvers to benefit from:
  - their properties
  - the implementation... already done, tested, optimized
  - connection between our framework and classical problems

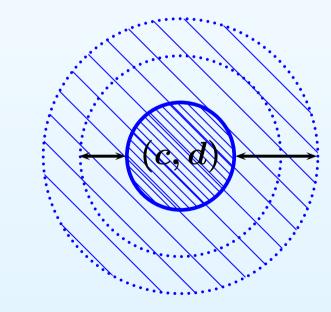
$$\begin{array}{ccc} c & \leadsto & (c,f) \\ C & \leadsto & (C,A,F,t) \end{array}$$

where, at the constraint's level:

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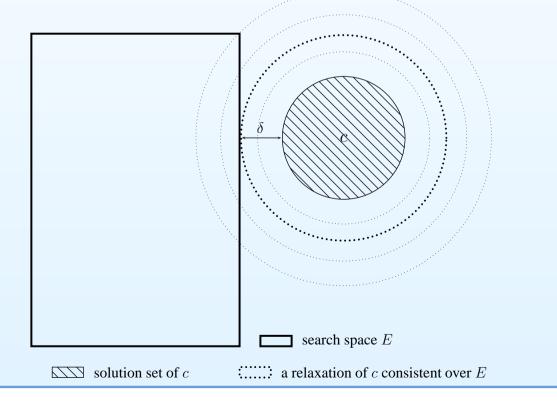
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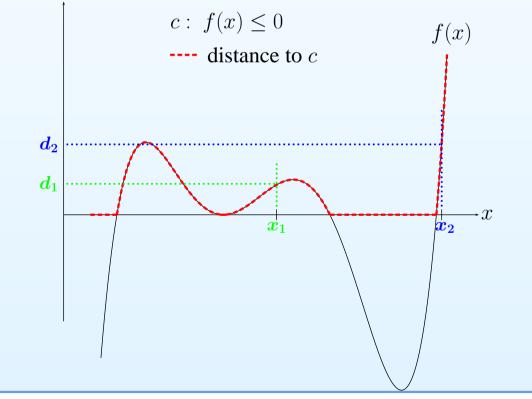
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• *f* stands for any error function: *distance, stair function, etc.* 

**Optimization:** minimization of error

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and when it comes to sets of constraints  $C = (c_1, \ldots, c_n)$ :

• 
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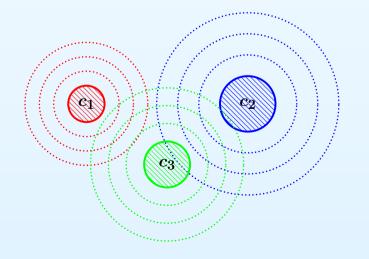
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and when it comes to sets of constraints  $C = (c_1, \ldots, c_n)$ :

- $F = (f_1, \ldots, f_n)$
- A is a vector of aggregation operators

e.g.,  $a = f_1 + \dots + f_n$ 

**Optimization:** minimization of the global error  $a(f_1, \ldots, f_n)$ 

$$\begin{array}{ccc} c & \leadsto & (c,f) \\ C & \leadsto & (C,A,F,t) \end{array}$$

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and when it comes to sets of constraints  $C = (c_1, \ldots, c_n)$ :

- $F = (f_1, \ldots, f_n)$
- A is a vector of aggregation operators
- t is a tree representing the order over constraints

Constrained optimization:

minimization of the error while satisfying the order

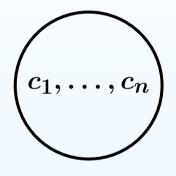
A few more words on  $\boldsymbol{A}$  and  $\boldsymbol{t}...$ 

A few more words on  $\boldsymbol{A}$  and t...

• t a tree of (sets of) constraints, defining the order over constraints

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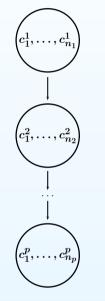
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• No order

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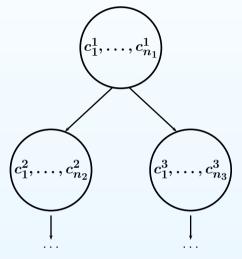
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- (Linear) Hierarchies of constraints: level 1 preferred to level 2, and so on and so forth...
- Priorities over (sets of) constraints: if level 1 can be satisfied, then try to satisfy level 2 too, etc. if level 1 inconsistent, no solution...

A few more words on  $\boldsymbol{A}$  and t...

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 (More complex) Hierarchies: general tree each edge stands for the parent being preferred to the children

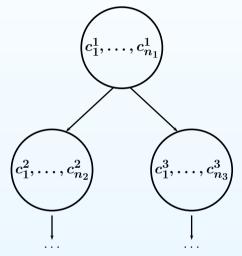
for 
$$k = 2, 3, \forall i \in \{1, \dots, n_1\}, j_k \in \{1, \dots, n_k\}, f_i^1(x) \leq f_{j_k}^k(x)$$

and / or:

for 
$$k = 2, 3, a_1(f_1^1(x), \dots, f_{n_1}^1) \leqslant a_k(f_1^k(x), \dots, f_{n_k}^k)$$

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 $^{\circ}$  "if ... then ... else ... " constraint structure: binary tree

$$\begin{array}{ccc} \text{if } c_1^1 \wedge \dots \wedge c_{n_1}^1 & \text{then} & (c_1^1 \wedge \dots \wedge c_{n_1}^1) \wedge (c_1^2 \wedge \dots \wedge c_{n_2}^2) \\ & \text{else} & c_1^3 \wedge \dots \wedge c_{n_3}^3 \end{array}$$

Problem with this scheme: may lead to inconsistencies too...

A few more words on  $\boldsymbol{A}$  and  $\boldsymbol{t}...$ 

- t a tree of (sets of) constraints, defining the order over constraints
- *A* a vector of aggregation operators

$$A = (\mathbf{a_0}, a_1, \dots, a_p)$$

*a*<sub>0</sub> is a global aggregation operator, possibly not defined (→ flag "?")
 (*a*<sub>1</sub>,...,*a<sub>p</sub>*) is a vector of additional aggreg. op., possibly empty

A few more words on  $\boldsymbol{A}$  and t...

- t a tree of (sets of) constraints, defining the order over constraints
- *A* a vector of aggregation operators **For instance:** 
  - $\circ A = (a_0)$  when there is no order, i.e., t=single node tree

•  $A = (?, a_1, ..., a_p)$  when t consists of p nodes e.g., constraint hierarchies

 $\circ A = (a_0)$  and t has p nodes: strong hierarchy

• A = (?) and t has p nodes: depending on the structure of t, interpreted as "linear" priority or "if ... then ... else ... "

Stretching the constraints:

$$(C, (a_0 = \sum), (d_1, \ldots, d_n), t_1 = \overset{(c_1, \ldots, c_n)}{\longrightarrow})$$

Stretching the constraints:  $(C, (a_0 = \sum), (d_1, \dots, d_n), t_1 = \bigcirc)$ 

Hierarchy of constraints:

$$(C, (?, a_1, \dots, a_p), (d_1, \dots, d_n), t_2 = \bigcup_{\substack{i_1, \dots, i_n \\ i_1, \dots, i_n \\ i_n \\$$

here each level has its aggregated value smaller than lower levels

Stretching the constraints:  $(C, (a_0 = \sum), (d_1, \dots, d_n), t_1 = \bigcirc^{(a_1, \dots, a_n)})$ Hierarchy of constraints: 1.  $(C, (?, a_1, \dots, a_p), (d_1, \dots, d_n), t_2 = \bigcirc^{(a_1, \dots, a_n)})$ 

Hierarchy of constraints:

$$(C, (a_0), (d_1, \dots, d_n), t_2 = \overset{(c_1, \dots, c_n)}{\underbrace{(c_1^2, \dots, c_n^2)}}$$

here we minimize  $a_0(x)$  under  $d_i^j(x) \leq d_k^l(x)$  for all i < j: stronger than former hierarchy scheme

Stretching the constraints:  $(C, (a_0 = \sum), (d_1, \dots, d_n), t_1 = \overset{(e_1, \dots, e_n)}{\longrightarrow})$ Hierarchy of constraints: 1.  $(C, (?, a_1, \dots, a_p), (d_1, \dots, d_n), t_2 = \overset{(e_1, \dots, e_n)}{\longrightarrow})$ here each level has its aggregated value smaller than lower levels 2.  $(C, (a_0), (d_1, \dots, d_n), t_2)$ here we minimize  $a_0(x)$  under  $d_i^j(x) \leq d_k^l(x)$  for all i < j

#### Tree structures:

$$(C, (?, a_1, \dots, a_p), (d_1, \dots, d_n), t_3 = \underbrace{(a_1, \dots, a_n)}_{(a_1, \dots, a_n)}$$
or  $(a_0)$ 

extension of the former linear hierarchy schemes (1, 2)

Stretching the constraints:  $(C, (a_0 = \sum), (d_1, \dots, d_n), t_1 = \bigcirc$ Hierarchy of constraints: 1.  $(C, (?, a_1, \dots, a_p), (d_1, \dots, d_n), t_2 = \bigcirc$ here each level has its aggregated value smaller than lower levels 2.  $(C, (a_0), (d_1, \dots, d_n), t_2)$ here we minimize  $a_0(x)$  under  $d_i^j(x) \leq d_k^l(x)$  for all i < jTree structures:  $(C, (?, a_1, \dots, a_p) or(a_0), (d_1, \dots, d_n), t_3 = \bigcirc$ extension of the former linear hierarchy schemes (1, 2)

"If then else" structures:

$$(C, (?), (d_1, \dots, d_n), t_3 = (t_1, \dots, t_n))$$

constraint satisfaction only: degenerate optimization problem

We can still...

• set weights on constraints

$$(C, \sum, (d_{w_1}, \dots, d_{w_n}), t = t_1)$$

• value the elements of the search space all appropriate functions f associated to constraints are allowed

# **Remaining issues**

### Issues

- Modeling language
- New aggregation operators
- Provide a semantics to the solution set of:
  - prioritized clusters of constraints,
  - partial orders over prioritized constraints

• What kind of output?

# Modeling language

- choose a <u>standard</u> language (*i.e.*, AMPL or any other language commonly used as input of classical solvers):
  - we may need to extend such a language, yet keeping easily useable and standard
- expressive enough to model soft constraints precisely (no ambiguity left)
  - possibly adjust the framework (data structure)
  - we have to make clear the correspondence between modeling and solutions: the user should get what s/he expects

Expressiveness of the modeling language

Associating values to constraints is ambiguous

 does it define the aggregation operator? weights ~> weighted sum, valued CSP

 $a(d_1(x),\ldots,d_n(x)) = w_1 \times d_1(x) + \cdots + w_n \times d_n(x)$ 

• or does it define an order : as preference levels for instance

$$(c_1,5), (c_2,3) \stackrel{?}{\Leftrightarrow} c_1 \succ c_2$$

but then what kind of preference: crisp? soft?

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We need slightly more detail, *e.g.*, a "code" specifying the use of an order and the kind of this order

is a tree expressive enough?

# New aggregation operators

 Idea: benefit from the Multi-Criteria Decision Making (MCDM) techniques

- no linear aggregation: weighted sum assume linear independence
- criteria are aggregated using integrals (Choquet, Sugeno), usually discretized

Improve the semantics of prioritized constraints

Generalize the total-order scheme to more complex ones.

# Improve the semantics of prioritized constraints

Generalize the total-order scheme to more complex ones.

#### **Problems so far:**

if more than one branch of priority (or a tree for instance), what is a solution?

- a max-length consistent branch?
- all consistent branches?
- should we establish an order over different branches? but then wouldn't we restrict ourselves too much?

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Generalize the total-order scheme to more complex ones.

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#### These points constitute perspectives for this project

What kind of output?

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- solutions of the optimization problem
- what if no solution? or too many?
  - should we provide users with suggestions? use of qualitative information before the solving process? or after?
  - should we run additional models in case of inconsistency?

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- what if no solution? or too many?
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#### Need for clear definition of the output:

may be adjusted when experiments are carried out on real problems

# Conclusion and Plans for future work

# Conclusion

### Already done

- definition of the framework for soft constraints we are going to use in this project
  - yet, adjustments are still possible
- prototype using this framework:
  - tested on inconsistent camera positioning problems
  - using classical constraint and optimization solvers: we benefit from their algorithmic power

# Plans for future work in Sakura

- implement a common prototype
  - probably on top of elisa: constraint solver implemented at LINA
- determine the user needs: experiments on GUI problems
  - <sup>o</sup> perform experiments on Pr. Hosobe's set of GUI problems
  - <sup>o</sup> adjust our solving algorithms w.r.t. these experiments
  - get preliminary feed-back
- explore possible connections with methods from MCDM
  - expressiveness may be improved using such techniques

# Plans for future work in Sakura (cont'd)

- apply models different from hierarchies to GUI problems
- extend our target application field (GUI)
- other projects of SCooP
  - integrate flexibility in speculative constraint processing
  - benefit from the work performed in the area of dynamic constraints (e.g., explanations)
- user interface
  - appropriate modelling language
  - easy-to-use interface

# The end

# Thank you for your attention

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